

# Cryptographic Hash Functions

## CSS441: Security and Cryptography

Sirindhorn International Institute of Technology  
Thammasat University

Prepared by Steven Gordon on 20 December 2015  
`css441y15s2l09, Steve/Courses/2015/s2/css441/lectures/cryptographic-hash-functions.tex, r4295`

# Contents

Hash Functions

Authentication

Signatures

Requirements

MD5 and SHA

## Hash Functions

## Authentication with Hash Functions

## Digital Signatures

## Requirements and Security

## MD5 and SHA

# Hash Functions

## Hash Functions

### Hash Functions

### Authentication

### Signatures

### Requirements

### MD5 and SHA

- ▶ **Hash function**  $H$ : variable-length block of data  $M$  input; fixed-size hash value  $h = H(M)$  output
- ▶ Applying  $H$  to large set of inputs should produce evenly distributed and random looking outputs
- ▶ **Cryptographic hash function**: computationally infeasible to find:
  1.  $M$  that maps to known  $h$  (one-way property)
  2.  $M_1$  and  $M_2$  that produce same  $h$  (collision-free property)
- ▶ Used to determine whether or not data has changed
- ▶ Examples: message authentication, digital signatures, one-way password file, intrusion/virus detection, PRNG

# Cryptographic Hash Function

## Hash Functions

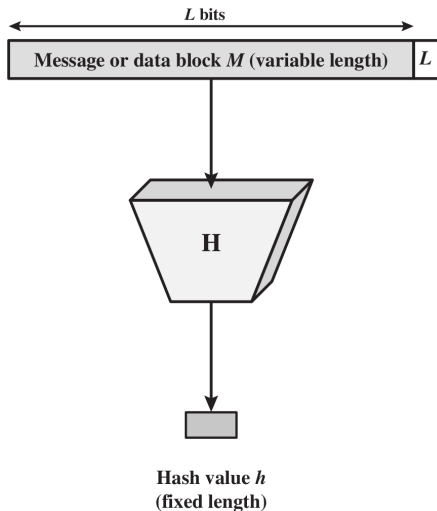
### Hash Functions

#### Authentication

#### Signatures

#### Requirements

#### MD5 and SHA



Credit: Figure 11.1 in Stallings, *Cryptography and Network Security*, 5th Ed., Pearson 2011

# Contents

Hash Functions

**Authentication**

Signatures

Requirements

MD5 and SHA

Hash Functions

**Authentication with Hash Functions**

Digital Signatures

Requirements and Security

MD5 and SHA

# Message Authentication

- ▶ Verify the integrity of a message
  - ▶ Ensure data received are exactly as sent
  - ▶ Assure identity of the sender is valid
- ▶ Hash function used to provide message authentication called **message digest**

# Message Authentication Example (a)

## Hash Functions

## Hash Functions

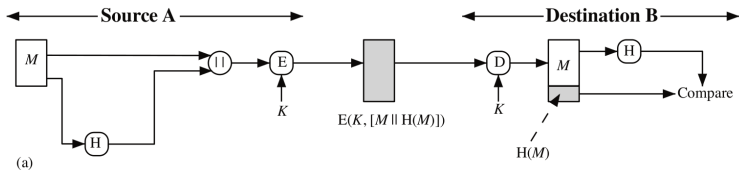
## Authentication

## Signatures

## Requirements

## MD5 and SHA

- ▶ Encrypt the message and hash code using symmetric encryption



# Message Authentication Example (b)

## Hash Functions

## Hash Functions

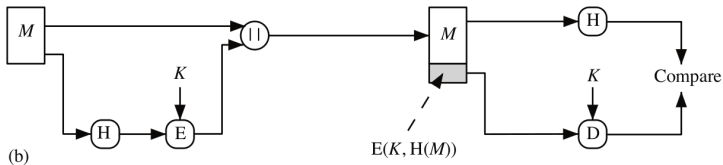
## Authentication

## Signatures

## Requirements

## MD5 and SHA

- ▶ Encrypt only hash code
- ▶ Reduces computation overhead when confidentiality not required





# Message Authentication Example (c)

## Hash Functions

## Hash Functions

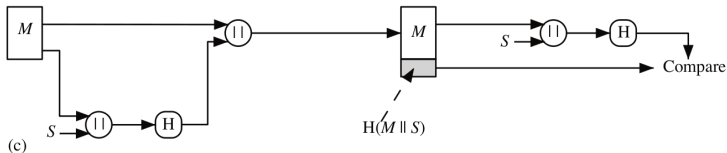
## Authentication

## Signatures

## Requirements

## MD5 and SHA

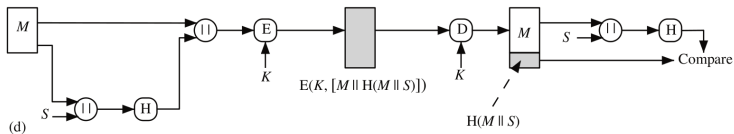
- ▶ Shared secret  $S$  is hashed
- ▶ No encryption needed



# Message Authentication Example (d)

## Hash Functions

- ▶ Shared secret combined with confidentiality



# Authentication and Encryption

## Hash Functions

## Hash Functions

## Authentication

## Signatures

## Requirements

## MD5 and SHA

- ▶ Sometimes desirable to avoid encryption when performing authentication
  - ▶ Encryption in software can be slow
  - ▶ Encryption in hardware has financial costs
  - ▶ Encryption hardware can be inefficient for small amounts of data
  - ▶ Encryption algorithms may be patented, increasing costs to use
- ▶ **Message Authentication Codes** (or keyed hash function)
  - ▶ Take secret key  $K$  and message  $M$  as input; produce hash (or MAC) as output
  - ▶ Combining hash function and encryption produces same result as MAC; but MAC algorithms can be more efficient than encryption algorithms
  - ▶ MAC covered in next topic

# Contents

Hash Functions

Authentication

**Signatures**

Requirements

MD5 and SHA

Hash Functions

Authentication with Hash Functions

Digital Signatures

Requirements and Security

MD5 and SHA

# Digital Signatures

- ▶ Aim of a signature: prove to anyone that a message originated at (or is approved by) a particular user
- ▶ Symmetric key cryptography
  - ▶ Two users,  $A$  and  $B$ , share a secret key  $K$
  - ▶ Receiver of message (user  $A$ ) can verify that message came from the other user ( $B$ )
  - ▶ User  $C$  *cannot* prove that the message came from  $B$  (it may also have come from  $A$ )
- ▶ Public key cryptography can provide signature: only one user has the private key

# Digital Signature Operations (Concept)

## Signing

- ▶ User signs a message by encrypting with own private key

$$S = E(PR_A, M)$$

- ▶ User attaches signature to message

## Verification

- ▶ User verifies a message by decrypting signature with signer's public key

$$M' = D(PU_A, S)$$

- ▶ User then compares received message  $M$  with decrypted  $M'$ ; if identical, signature is verified

# Digital Signature Operations (Practice)

No need to encrypt entire message; encrypt hash of message

## Signing

- ▶ User signs a message by encrypting **hash of message** with own private key

$$S = E(PR_A, H(M))$$

- ▶ User attaches signature to message

## Verification

- ▶ User verifies a message by decrypting signature with signer's public key

$$h = D(PU_A, S)$$

- ▶ User then compares **hash of** received message,  $H(M)$ , with decrypted  $h$ ; if identical, signature is verified

# Digital Signature Algorithms

- ▶ RSA
- ▶ Digital Signature Algorithm (DSA): FIPS-186
- ▶ ECDSA: DSA with elliptic curve cryptography
- ▶ ElGamal signature scheme: DSA is enhancement of ElGamal
- ▶ Bilinear pairing based signatures, e.g. BLS
- ▶ Different hash algorithms can be used; e.g. SHA2
  - ▶ Pre-image resistant, second pre-image resistant, collision resistant



# Contents

Hash Functions

Authentication

Signatures

**Requirements**

MD5 and SHA

Hash Functions

Authentication with Hash Functions

Digital Signatures

**Requirements and Security**

MD5 and SHA

## Pre-images and Collisions

- ▶ For hash value  $h = H(x)$ ,  $x$  is **pre-image** of  $h$
- ▶  $H$  is a many-to-one mapping;  $h$  has multiple pre-images
- ▶ **Collision** occurs if  $x \neq y$  and  $H(x) = H(y)$
- ▶ Collisions are undesirable
- ▶ How many pre-images for given hash value?
  - ▶ If  $H$  takes  $b$ -bit input block,  $2^b$  possible messages
  - ▶ For  $n$ -bit hash code, where  $b > n$ ,  $2^n$  possible hash codes
  - ▶ On average, if uniformly distributed hash values, then each hash value has  $2^{b-n}$  pre-images

# Requirements of Cryptographic Hash Function

**Variable input size:**  $H$  can be applied to input block of any size

**Fixed output size:**  $H$  produces fixed length output

**Efficiency:**  $H(x)$  relatively easy to compute (practical implementations)

**Pre-image resistant:** For any given  $h$ , computationally infeasible to find  $y$  such that  $H(y) = h$  (*one-way property*)

**Second pre-image resistant:** For any given  $x$ , computationally infeasible to find  $y \neq x$  with  $H(y) = H(x)$  (*weak collision resistant*)

**Collision resistant:** Computationally infeasible to find any pair  $(x, y)$  such that  $H(x) = H(y)$  (*strong collision resistant*)

**Pseudo-randomness:** Output of  $H$  meets standard tests for pseudo-randomness

# Required Hash Properties for Different Applications

**Weak hash function:** Satisfies first 5 requirements (but not collision resistant)

**Strong hash function:** Also collision resistant

	<b>Preimage Resistant</b>	<b>Second Preimage Resistant</b>	<b>Collision Resistant</b>
Hash + digital signature	yes	yes	yes*
Intrusion detection and virus detection		yes	
Hash + symmetric encryption			
One-way password file	yes		
MAC	yes	yes	yes*

\* Resistance required if attacker is able to mount a chosen message attack

Credit: Table 11.2 in Stallings, *Cryptography and Network Security*, 5th Ed., Pearson 2011

# Brute Attacks on Hash Functions

## Pre-image and Second Pre-image Attack

- ▶ Find a  $y$  that gives specific  $h$ ; try all possible values of  $y$
- ▶ With  $m$ -bit hash code, effort required proportional to  $2^m$

## Collision Resistant Brute Attack

- ▶ Find any two messages that have same hash values
- ▶ Effort required is proportional to  $2^{m/2}$
- ▶ Due to **birthday paradox**, easier than pre-image attacks

## Practical Effort

- ▶ Cryptanalysis attacks possible in theory; complex
- ▶ Collision resistance desirable for general hash algorithms
- ▶ MD5 uses 128-bits: collision attacks possible ( $2^{60}$ )
- ▶ SHA uses longer codes; collision attacks infeasible

# Contents

Hash Functions

Authentication

Signatures

Requirements

MD5 and SHA

Hash Functions

Authentication with Hash Functions

Digital Signatures

Requirements and Security

MD5 and SHA

- ▶ Message Digest algorithm 5, developed by Ron Rivest in 1991
- ▶ Standardised by IETF in RFC 1321
- ▶ Generates 128-bit hash
- ▶ Was commonly used by applications, passwords, file integrity; **no longer recommended**
- ▶ Collision and other attacks possible; tools publicly available to attack MD5

# SHA

## Hash Functions

Hash Functions

Authentication

Signatures

Requirements

MD5 and SHA

- ▶ Secure Hash Algorithm, developed by NIST
- ▶ Standardised by NIST in FIPS 180 in 1993
- ▶ Improvements over time: SHA-0, SHA-1, SHA-2, SHA-3
- ▶ SHA-1 (and SHA-0) are considered insecure; **no longer recommended**
- ▶ SHA-3 in development, competition run by NIST

	SHA-1	SHA-224	SHA-256	SHA-384	SHA-512
<b>Message Digest Size</b>	160	224	256	384	512
<b>Message Size</b>	$< 2^{64}$	$< 2^{64}$	$< 2^{64}$	$< 2^{128}$	$< 2^{128}$
<b>Block Size</b>	512	512	512	1024	1024
<b>Word Size</b>	32	32	32	64	64
<b>Number of Steps</b>	80	64	64	80	80

Credit: Table 11.3 in Stallings, *Cryptography and Network Security*, 5th Ed., Pearson 2011