

Block Ciphers and DES

CSS441: Security and Cryptography

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Simplified-DES

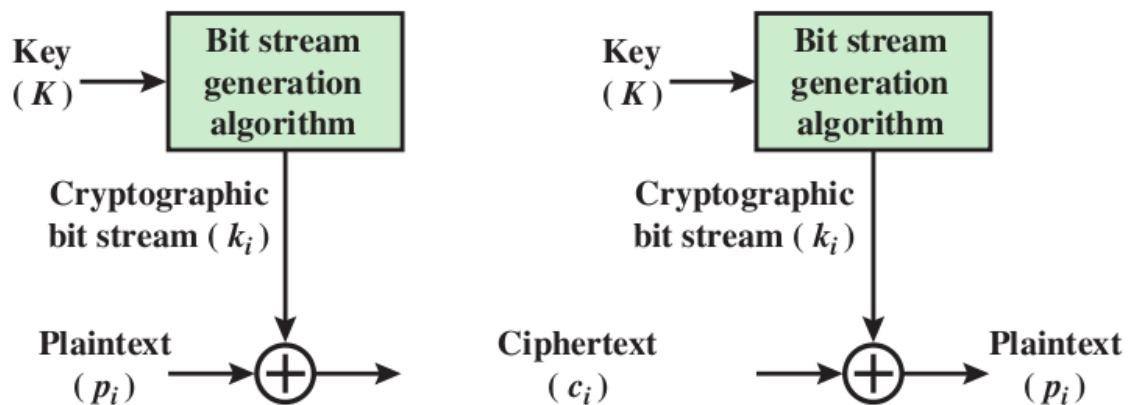
DES Details

DES Design Issues and Attacks

3DES, AES and Other Block Ciphers

Stream Ciphers

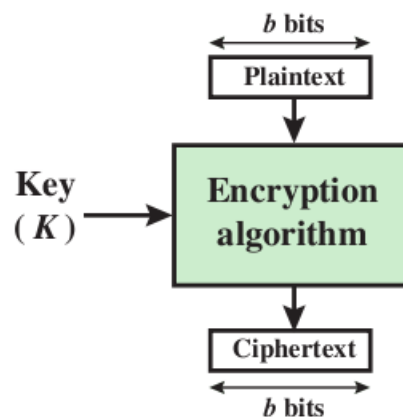
- ▶ Encrypts a digital data stream one bit or one byte at a time
- ▶ One time pad is example; but practical limitations
- ▶ Typical approach for stream cipher:
 - ▶ Key (K) used as input to bit-stream generator algorithm
 - ▶ Algorithm generates cryptographic bit stream (k_i) used to encrypt plaintext
 - ▶ Users share a key; use it to generate keystream



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Block Ciphers

- ▶ Encrypt a block of plaintext as a whole to produce same sized ciphertext
- ▶ Typical block sizes are 64 or 128 bits
- ▶ Modes of operation used to apply block ciphers to larger plaintexts



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Reversible and Irreversible Mappings

- ▶ n -bit block cipher takes n bit plaintext and produces n bit ciphertext
- ▶ 2^n possible different plaintext blocks
- ▶ Encryption must be reversible (decryption possible)
- ▶ Each plaintext block must produce unique ciphertext block
- ▶ Total transformations is $2^n!$

Reversible Mapping		Irreversible Mapping	
Plaintext	Ciphertext	Plaintext	Ciphertext
00	11	00	11
01	10	01	10
10	00	10	01
11	01	11	01

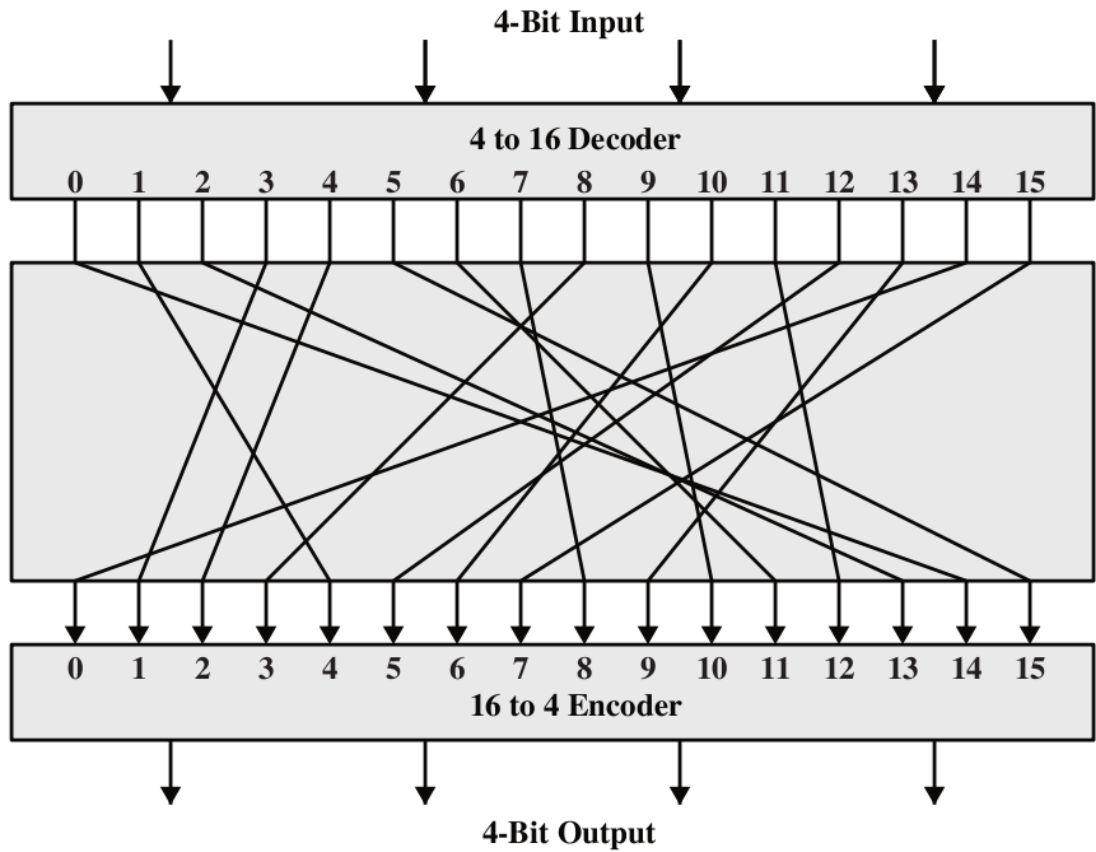
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Ideal Block Cipher

- ▶ n -bit input maps to 2^n possible input states
- ▶ Substitution used to produce 2^n output states
- ▶ Output states map to n -bit output
- ▶ Ideal block cipher allows maximum number of possible encryption mappings from plaintext block
- ▶ Problems with ideal block cipher:
 - ▶ Small block size: equivalent to classical substitution cipher; cryptanalysis based on statistical characteristics feasible
 - ▶ Large block size: key must be very large; performance/implementation problems

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General Block Substitution



Encryption/Decryption Tables

Plaintext	Ciphertext
0000	1110
0001	0100
0010	1101
0011	0001
0100	0010
0101	1111
0110	1011
0111	1000
1000	0011
1001	1010
1010	0110
1011	1100
1100	0101
1101	1001
1110	0000
1111	0111

Ciphertext	Plaintext
0000	1110
0001	0011
0010	0100
0011	1000
0100	0001
0101	1100
0110	1010
0111	1111
1000	0111
1001	1101
1010	1001
1011	0110
1100	1011
1101	0010
1110	0000
1111	0101

Feistel Structure for Block Ciphers

- ▶ Feistel proposed applying two or more simple ciphers in sequence so final result is cryptographically stronger than component ciphers
- ▶ n -bit block length; k -bit key length; 2^k transformations
- ▶ Feistel cipher alternates: substitutions, transpositions (permutations)
- ▶ Applies concepts of diffusion and confusion
- ▶ Applied in many ciphers today
- ▶ Approach:
 - ▶ Plaintext split into halves
 - ▶ Subkeys (or round keys) generated from key
 - ▶ Round function, F , applied to right half
 - ▶ Apply substitution on left half using XOR
 - ▶ Apply permutation: interchange to halves

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Diffusion and Confusion

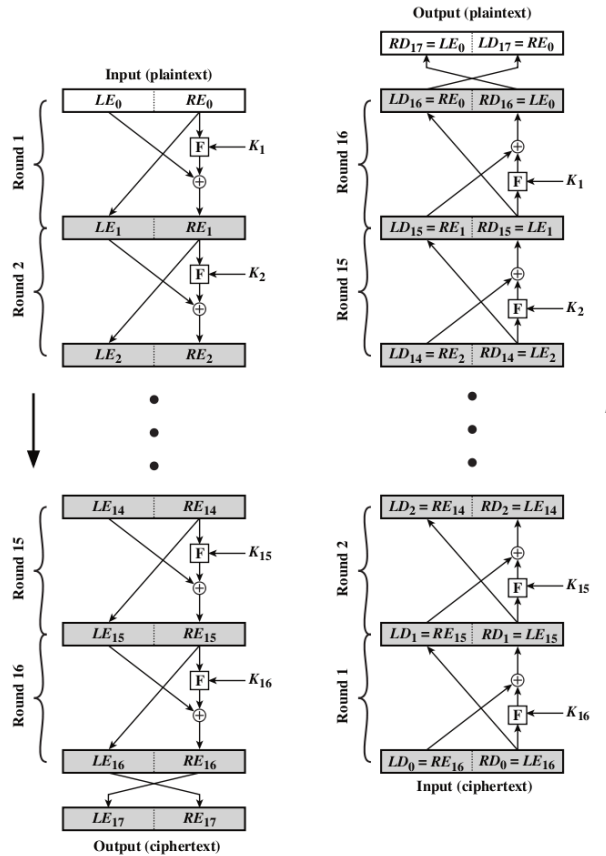
Diffusion

- ▶ Statistical nature of plaintext is reduced in ciphertext
- ▶ E.g. A plaintext letter affects the value of many ciphertext letters
- ▶ How: repeatedly apply permutation (transposition) to data, and then apply function

Confusion

- ▶ Make relationship between ciphertext and key as complex as possible
- ▶ Even if attacker can find some statistical characteristics of ciphertext, still hard to find key
- ▶ How: apply complex (non-linear) substitution algorithm

Feistel Encryption and Decryption



Using the Feistel Structure

- ▶ Exact implementation depends on various design features
 - ▶ Block size, e.g. 64, 128 bits: larger values leads to more diffusion
 - ▶ Key size, e.g. 128 bits: larger values leads to more confusion, resistance against brute force
 - ▶ Number of rounds, e.g. 16 rounds
 - ▶ Subkey generation algorithm: should be complex
 - ▶ Round function F : should be complex
- ▶ Other factors include fast encryption in software and ease of analysis
- ▶ Trade-off: security vs performance

Feistel Example

Principles

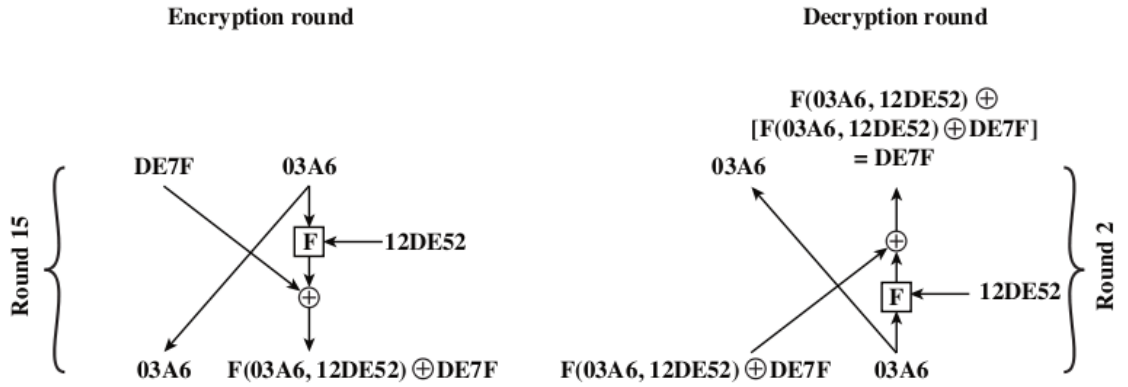
DES

S-DES

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DES Design

Other Ciphers



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3DES, AES and Other Block Ciphers

Data Encryption Standard

- ▶ Symmetric block cipher
 - ▶ 56-bit key, 64-bit input block, 64-bit output block
- ▶ One of most used encryption systems in world
 - ▶ Developed in 1977 by NBS/NIST
 - ▶ Designed by IBM (Lucifer) with input from NSA
 - ▶ Principles used in other ciphers, e.g. 3DES, IDEA
- ▶ Simplified DES (S-DES)
 - ▶ Cipher using principles of DES
 - ▶ Developed for education (not real world use)

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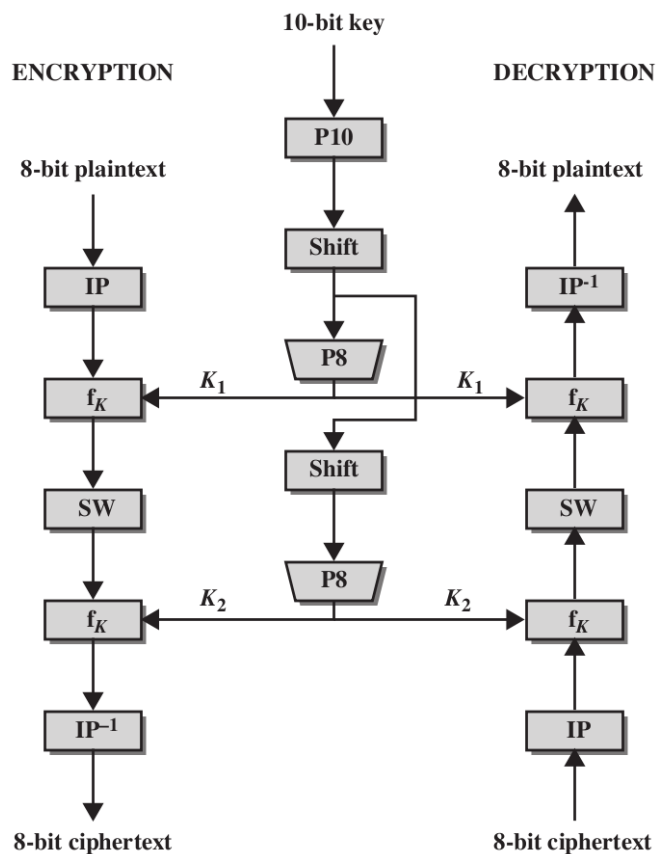
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Simplified DES

- ▶ Input (plaintext) block: 8-bits
- ▶ Output (ciphertext) block: 8-bits
- ▶ Key: 10-bits
- ▶ Rounds: 2
- ▶ Round keys generated using permutations and left shifts
- ▶ Encryption: initial permutation, round function, switch halves
- ▶ Decryption: Same as encryption, except round keys used in opposite order

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S-DES Algorithm



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S-DES Operations

► P10 (permutate)

Input : 1 2 3 4 5 6 7 8 9 10

Output: 3 5 2 7 4 10 1 9 8 6

► P8 (select and permutate)

Input : 1 2 3 4 5 6 7 8 9 10

Output: 6 3 7 4 8 5 10 9

► P4 (permutate)

Input : 1 2 3 4

Output: 2 4 3 1

S-DES Operations

► EP (expand and permutate)

Input : 1 2 3 4

Output: 4 1 2 3 2 3 4 1

► IP (initial permutation)

Input : 1 2 3 4 5 6 7 8

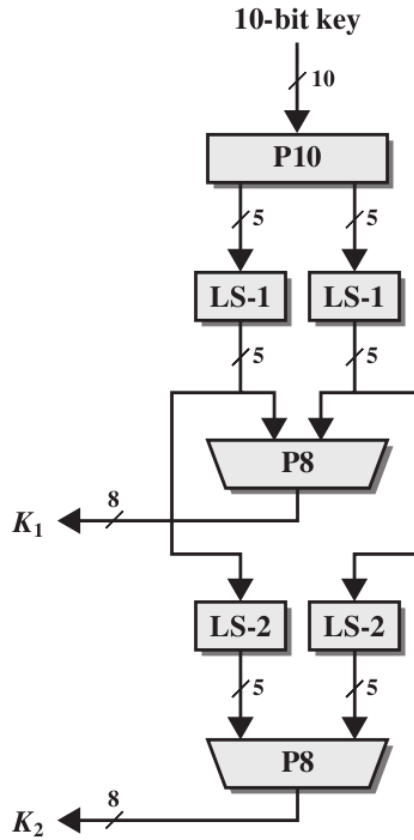
Output: 2 6 3 1 4 8 5 7

► IP^{-1} (inverse of IP)

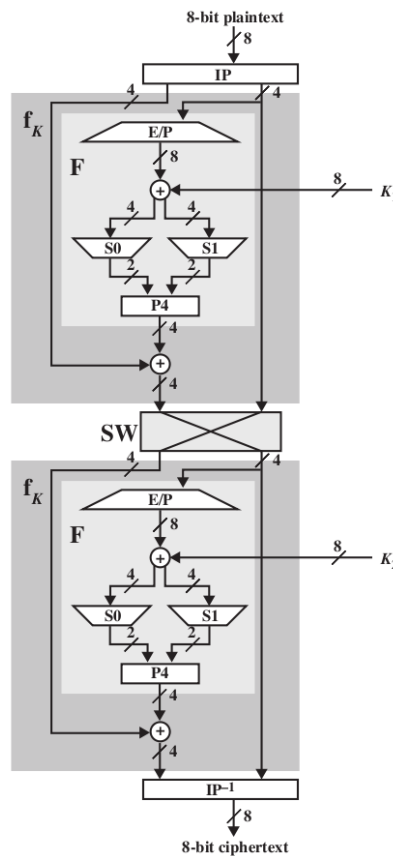
► LS-1 (left shift 1 position)

► LS-2 (left shift 2 positions)

S-DES Key Generation



S-DES Encryption Details



S-DES S-Boxes

- ▶ S-DES (and DES) perform substitutions using S-Boxes
- ▶ S-Box considered as a matrix: input used to select row/column; selected element is output
- ▶ 4-bit input: $bit_1, bit_2, bit_3, bit_4$
- ▶ $bit_1 bit_4$ specifies row (0, 1, 2 or 3 in decimal)
- ▶ $bit_2 bit_3$ specifies column
- ▶ 2-bit output

$$S_0 = \begin{bmatrix} 01 & 00 & 11 & 10 \\ 11 & 10 & 01 & 00 \\ 00 & 10 & 01 & 11 \\ 11 & 01 & 11 & 10 \end{bmatrix} \quad S_1 = \begin{bmatrix} 00 & 01 & 10 & 11 \\ 10 & 00 & 01 & 11 \\ 11 & 00 & 01 & 00 \\ 10 & 01 & 00 & 11 \end{bmatrix}$$

S-DES Example

- ▶ Plaintext: 01110010
- ▶ Key: 1010000010
- ▶ Ciphertext: 01110111

S-DES Summary

- ▶ Educational encryption algorithm
- ▶ S-DES expressed as functions:

$$ciphertext = IP^{-1} (f_{K_2} (SW (f_{K_1} (IP (plaintext))))))$$

$$plaintext = IP^{-1} (f_{K_1} (SW (f_{K_2} (IP (ciphertext))))))$$

- ▶ Security of S-DES:
 - ▶ 10-bit key, 1024 keys: brute force easy
 - ▶ If know plaintext and corresponding ciphertext, can we determine key? Very hard

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Comparing DES and S-DES

S-DES

- ▶ 8-bit blocks
- ▶ 10-bit key: 2 x 8-bit round keys
- ▶ IP: 8-bits
- ▶ F operates on 4 bits
- ▶ 2 S-Boxes
- ▶ 2 rounds

S-DES encryption:

$$ciphertext = IP^{-1} (f_{K_2} (SW (f_{K_1} (IP (plaintext))))))$$

DES encryption:

$$ciphertext = IP^{-1} (f_{K_{16}} (SW (f_{K_{15}} (SW (\dots (f_{K_1} (IP (plaintext))))))))$$

DES

- ▶ 64-bit blocks
- ▶ 56-bit key: 16 x 48-bit round keys
- ▶ IP: 64 bits
- ▶ F operates on 32 bits
- ▶ 8 S-Boxes
- ▶ 16 rounds

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Block Cipher Principles

The Data Encryption Standard

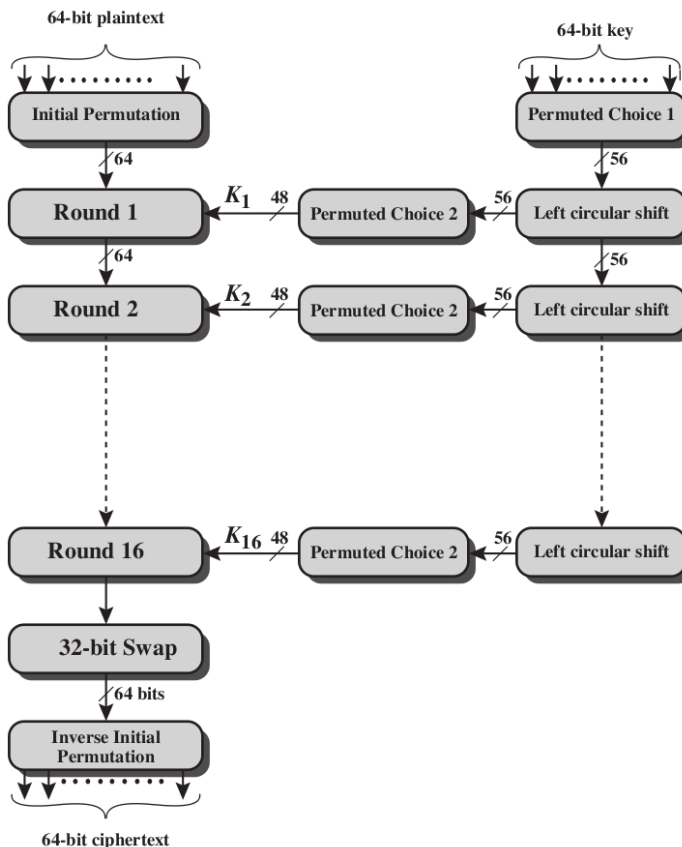
Simplified-DES

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3DES, AES and Other Block Ciphers

General DES Encryption Algorithm



Permutation Tables for DES

Block Ciphers

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Other Ciphers

(a) Initial Permutation (IP)

58	50	42	34	26	18	10	2
60	52	44	36	28	20	12	4
62	54	46	38	30	22	14	6
64	56	48	40	32	24	16	8
57	49	41	33	25	17	9	1
59	51	43	35	27	19	11	3
61	53	45	37	29	21	13	5
63	55	47	39	31	23	15	7

(b) Inverse Initial Permutation (IP⁻¹)

40	8	48	16	56	24	64	32
39	7	47	15	55	23	63	31
38	6	46	14	54	22	62	30
37	5	45	13	53	21	61	29
36	4	44	12	52	20	60	28
35	3	43	11	51	19	59	27
34	2	42	10	50	18	58	26
33	1	41	9	49	17	57	25

Permutation Tables for DES

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Other Ciphers

(c) Expansion Permutation (E)

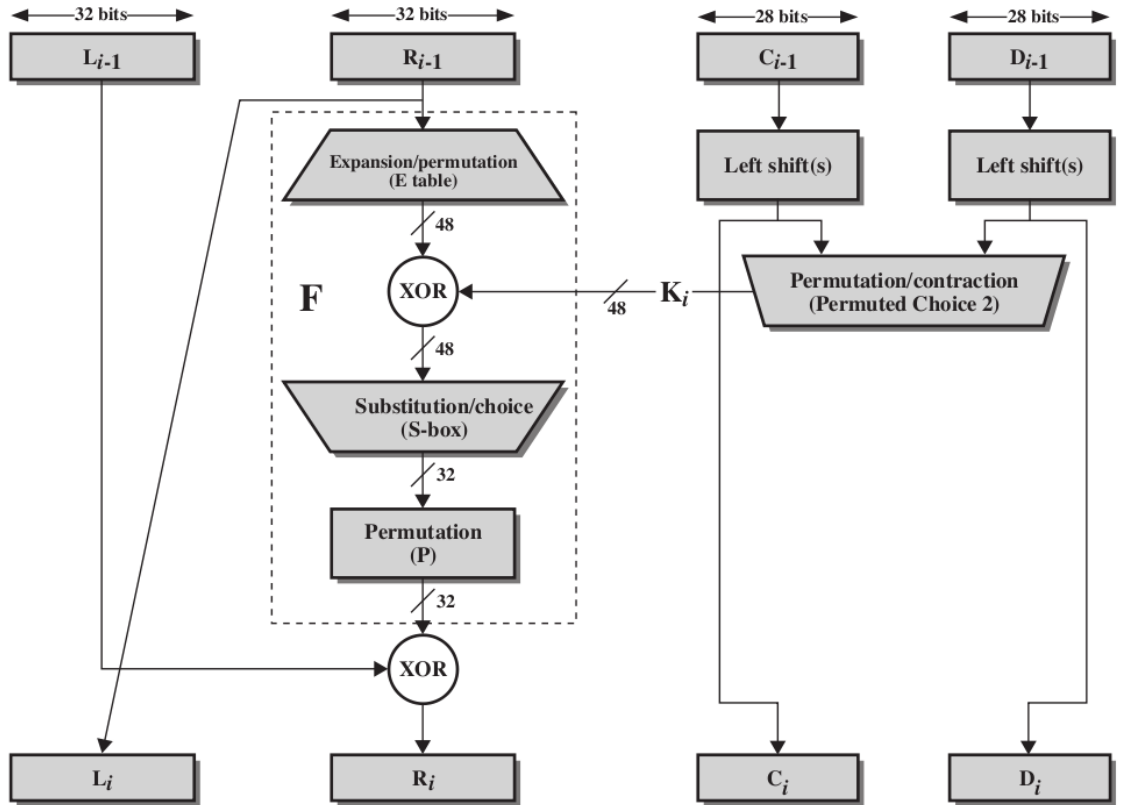
32	1	2	3	4	5
4	5	6	7	8	9
8	9	10	11	12	13
12	13	14	15	16	17
16	17	18	19	20	21
20	21	22	23	24	25
24	25	26	27	28	29
28	29	30	31	32	1

(d) Permutation Function (P)

16	7	20	21	29	12	28	17
1	15	23	26	5	18	31	10
2	8	24	14	32	27	3	9
19	13	30	6	22	11	4	25

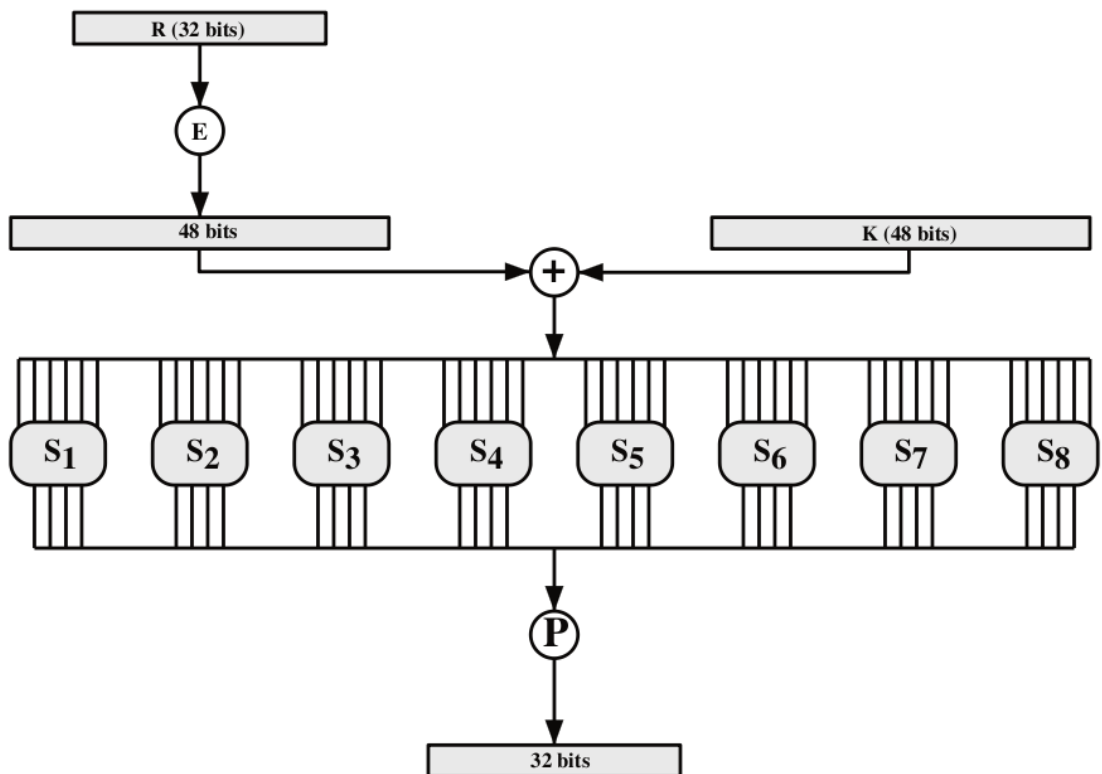
Single Round of DES Algorithm

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Calculation of $F(R,K)$

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Definition of DES S-Boxes

Block Ciphers

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Other Ciphers

S_1	14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
	0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8
	4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
	15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13
S_2	15	1	8	14	6	11	3	4	9	7	2	13	12	0	5	10
	3	13	4	7	15	2	8	14	12	0	1	10	6	9	11	5
	0	14	7	11	10	4	13	1	5	8	12	6	9	3	2	15
	13	8	10	1	3	15	4	2	11	6	7	12	0	5	14	9
S_3	10	0	9	14	6	3	15	5	1	13	12	7	11	4	2	8
	13	7	0	9	3	4	6	10	2	8	5	14	12	11	15	1
	13	6	4	9	8	15	3	0	11	1	2	12	5	10	14	7
	1	10	13	0	6	9	8	7	4	15	14	3	11	5	2	12
S_4	7	13	14	3	0	6	9	10	1	2	8	5	11	12	4	15
	13	8	11	5	6	15	0	3	4	7	2	12	1	10	14	9
	10	6	9	0	12	11	7	13	15	1	3	14	5	2	8	4
	3	15	0	6	10	1	13	8	9	4	5	11	12	7	2	14

Definition of DES S-Boxes

Block Ciphers

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Other Ciphers

S_5	2	12	4	1	7	10	11	6	8	5	3	15	13	0	14	9
	14	11	2	12	4	7	13	1	5	0	15	10	3	9	8	6
	4	2	1	11	10	13	7	8	15	9	12	5	6	3	0	14
	11	8	12	7	1	14	2	13	6	15	0	9	10	4	5	3
S_6	12	1	10	15	9	2	6	8	0	13	3	4	14	7	5	11
	10	15	4	2	7	12	9	5	6	1	13	14	0	11	3	8
	9	14	15	5	2	8	12	3	7	0	4	10	1	13	11	6
	4	3	2	12	9	5	15	10	11	14	1	7	6	0	8	13
S_7	4	11	2	14	15	0	8	13	3	12	9	7	5	10	6	1
	13	0	11	7	4	9	1	10	14	3	5	12	2	15	8	6
	1	4	11	13	12	3	7	14	10	15	6	8	0	5	9	2
	6	11	13	8	1	4	10	7	9	5	0	15	14	2	3	12
S_8	13	2	8	4	6	15	11	1	10	9	3	14	5	0	12	7
	1	15	13	8	10	3	7	4	12	5	6	11	0	14	9	2
	7	11	4	1	9	12	14	2	0	6	10	13	15	3	5	8
	2	1	14	7	4	10	8	13	15	12	9	0	3	5	6	11

DES Key Schedule Calculation

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Other Ciphers

(a) Input Key

1	2	3	4	5	6	7	8
9	10	11	12	13	14	15	16
17	18	19	20	21	22	23	24
25	26	27	28	29	30	31	32
33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48
49	50	51	52	53	54	55	56
57	58	59	60	61	62	63	64

(b) Permuted Choice One (PC-1)

57	49	41	33	25	17	9
1	58	50	42	34	26	18
10	2	59	51	43	35	27
19	11	3	60	52	44	36
63	55	47	39	31	23	15
7	62	54	46	38	30	22
14	6	61	53	45	37	29
21	13	5	28	20	12	4

(c) Permuted Choice Two (PC-2)

14	17	11	24	1	5	3	28
15	6	21	10	23	19	12	4
26	8	16	7	27	20	13	2
41	52	31	37	47	55	30	40
51	45	33	48	44	49	39	56
34	53	46	42	50	36	29	32

(d) Schedule of Left Shifts

Round Number	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Bits Rotated	1	1	2	2	2	2	2	2	1	2	2	2	2	2	2	1

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The Avalanche Effect

Aim: small change in key (or plaintext) produces large change in ciphertext

- ▶ Avalanche effect is present in DES (good for security)
- ▶ Following examples show the number of bits that change in output when two different inputs are used, differing by 1 bit
 - ▶ Plaintext 1: 02468aceeca86420
Plaintext 2: 12468aceeca86420
Ciphertext difference: 32 bits
 - ▶ Key 1: 0f1571c947d9e859
Key 2: 1f1571c947d9e859
Ciphertext difference: 30

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Avalanche Effect in DES: Change in Plaintext

Round		δ	Round		δ
	02468aceeca86420 12468aceeca86420	1	9	c11bfc09887fbc6c 99f911532eed7d94	32
1	3cf03c0fbad22845 3cf03c0fbad32845	1	10	887fbc6c600f7e8b 2eed7d94d0f23094	34
2	bad2284599e9b723 bad3284539a9b7a3	5	11	600f7e8bf596506e d0f23094455da9c4	37
3	99e9b7230bae3b9e 39a9b7a3171cb8b3	18	12	f596506e738538b8 455da9c47f6e3cf3	31
4	0bae3b9e42415649 171cb8b3ccaca55e	34	13	738538b8c6a62c4e 7f6e3cf34bc1a8d9	29
5	4241564918b3fa41 ccaca55ed16c3653	37	14	c6a62c4e56b0bd75 4bc1a8d91e07d409	33
6	18b3fa419616fe23 d16c3653cf402c68	33	15	56b0bd7575e8fd8f 1e07d4091ce2e6dc	31
7	9616fe2367117cf2 cf402c682b2cefbc	32	16	75e8fd8f25896490 1ce2e6dc365e5f59	32
8	67117cf2c11bfc09 2b2cefbc99f91153	33	IP ⁻¹	da02ce3a89ecac3b 057cde97d7683f2a	32

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Round		δ	Round		δ
	02468aceeca86420	0	9	c11bfc09887fbc6c	34
	02468aceeca86420			548f1de471f64dfd	
1	3cf03c0fbad22845	3	10	887fbc6c600f7e8b	36
	3cf03c0f9ad628c5			71f64dfd4279876c	
2	bad2284599e9b723	11	11	600f7e8bf596506e	32
	9ad628c59939136b			4279876c399fdc0d	
3	99e9b7230bae3b9e	25	12	f596506e738538b8	28
	9939136b768067b7			399fdc0d6d208dbb	
4	0bae3b9e42415649	29	13	738538b8c6a62c4e	33
	768067b75a8807c5			6d208dbbb9bdeea	
5	4241564918b3fa41	26	14	c6a62c4e56b0bd75	30
	5a8807c5488dbe94			b9bdeeaad2c3a56f	
6	18b3fa419616fe23	26	15	56b0bd7575e8fd8f	33
	488dbe94aba7fe53			d2c3a56f2765c1fb	
7	9616fe2367117cf2	27	16	75e8fd8f25896490	30
	aba7fe53177d21e4			2765c1fb01263dc4	
8	67117cf2c11bfc09	32	IP ⁻¹	da02ce3a89ecac3b	30
	177d21e4548f1de4			ee92b50606b62b0b	

Key Size

- ▶ Although 64 bit initial key, only 56 bits used in encryption (other 8 for parity check)
- ▶ $2^{56} = 7.2 \times 10^{16}$
 - ▶ 1977: estimated cost \$US20m to build machine to break in 10 hours
 - ▶ 1998: EFF built machine for \$US250k to break in 3 days
 - ▶ Today: 56 bits considered too short to withstand brute force attack
- ▶ 3DES uses 128-bit keys

Attacks on DES

Timing Attacks

- ▶ Information gained about key/plaintext by observing how long implementation takes to decrypt
- ▶ No known useful attacks on DES

Differential Cryptanalysis

- ▶ Observe how pairs of plaintext blocks evolve
- ▶ Break DES in 2^{47} encryptions (compared to 2^{55}); but require 2^{47} chosen plaintexts

Linear Cryptanalysis

- ▶ Find linear approximations of the transformations
- ▶ Break DES using 2^{43} known plaintexts

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DES Algorithm Design

DES was designed in private; questions about the motivation of the design

- ▶ S-Boxes provide non-linearity: important part of DES, generally considered to be secure
- ▶ S-Boxes provide increased confusion
- ▶ Permutation P chosen to increase diffusion

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Multiple Encryption with DES

- ▶ DES is vulnerable to brute force attack
- ▶ Alternative block cipher that makes use of DES software/equipment/knowledge: encrypt multiple times with different keys
- ▶ Options:
 1. Double DES: not much better than single DES
 2. Triple DES (3DES) with 2 keys: brute force 2^{112}
 3. Triple DES with 3 keys: brute force 2^{168}

Double Encryption

Block Ciphers

Principles

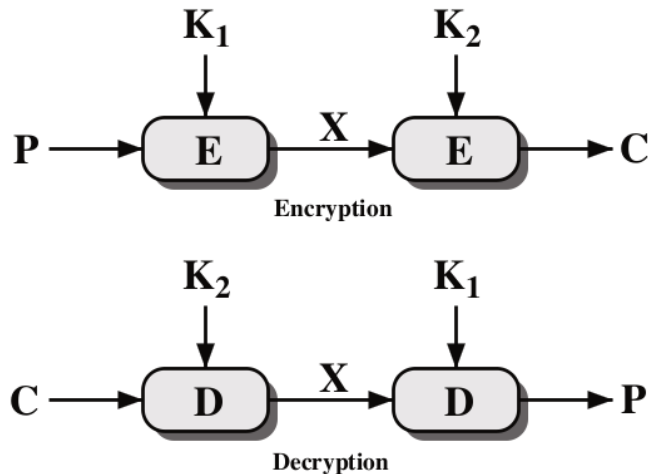
DES

S-DES

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Other Ciphers



- ▶ For DES, 2×56 -bit keys, meaning 112-bit key length
- ▶ Requires 2^{111} operations for brute force?
- ▶ Meet-in-the-middle attack makes it easier

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Meet-in-the-Middle Attack

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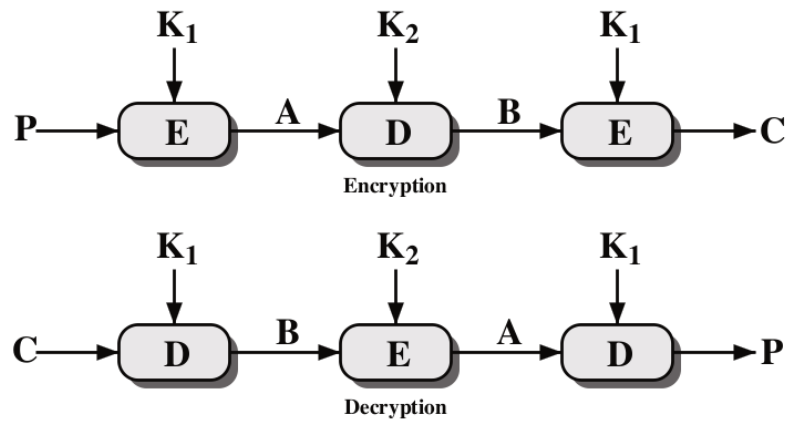
DES Design

Other Ciphers

- ▶ Double DES Encryption: $C = E(K_2, E(K_1, P))$
- ▶ Say $X = E(K_1, P) = D(K_2, C)$
- ▶ Attacker knows two plaintext, ciphertext pairs (P_a, C_a) and (P_b, C_b)
 1. Encrypt P_a using all 2^{56} values of K_1 to get multiple values of X
 2. Store results in table and sort by X
 3. Decrypt C_a using all 2^{56} values of K_2
 4. As each decryption result produced, check against table
 5. If match, check current K_1, K_2 on C_b . If P_b obtained, then accept the keys
- ▶ With two known plaintext, ciphertext pairs, probability of successful attack is almost 1
- ▶ Encrypt/decrypt operations required: 2^{56} (twice as many as single DES)

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Triple Encryption



- ▶ 2 keys, 112 bits
- ▶ 3 keys, 168 bits
- ▶ Why E-D-E? To be compatible with single DES:

$$C = E(K_1, D(K_1, E(K_1, P))) = E(K_1, P)$$

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Advanced Encryption Standard

- ▶ NIST called for proposals for new standard in 1997
 - ▶ Aims: security, efficient software/hardware implementations, low memory requirements, parallel processing
 - ▶ Candidate algorithms from around the world
 - ▶ Rijndael chosen, standard called AES created in 2001
- ▶ AES:
 - ▶ Block size: 128 bits (others possible)
 - ▶ Key size: 128, 192, 256 bits
 - ▶ Rounds: 10, 12, 14 (depending on key)
 - ▶ Operations: XOR with round key, substitutions using S-Boxes, mixing using Galois Field arithmetic
- ▶ Widely used in file encryption, network communications
- ▶ Generally considered secure
- ▶ See textbook for details (including S-AES)

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Other Symmetric Encryption Algorithms

- ▶ Blowfish (Schneier, 1993): 64 bit blocks/32–448 bit keys; Feistel structure
- ▶ Twofish (Schneier et al, 1998): 128/128, 192, 256; Feistel structure
- ▶ Serpent (Anderson et al, 1998): 128/128, 192, 256; Substitution-permutation network
- ▶ Camellia (Mitsubishi/NTT, 2000): 128/128, 192, 256; Feistel structure
- ▶ IDEA (Lai and Massey, 1991): 64/128
- ▶ CAST-128 (Adams and Tavares, 1996): 64/40–128; Feistel structure
- ▶ CAST-256 (Adams and Tavares, 1998): 128/up to 256; Feistel structure
- ▶ RC5 (Rivest, 1994): 32, 64 or 128/up to 2040; Feistel-like structure
- ▶ RC6 (Rivest et al, 1998): 128/128, 192, 256; Feistel structure

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Cryptanalysis on Block Ciphers

Cipher	Method	Key space	Time	Required resources:	
				Memory	Known data
DES	Brute force	2^{56}	2^{56}	-	-
3DES	MITM	2^{168}	2^{111}	2^{56}	2^2
3DES	Lucks	2^{168}	2^{113}	2^{88}	2^{32}
AES 128	Biclique	2^{128}	$2^{126.1}$	2^8	2^{88}
AES 256	Biclique	2^{256}	$2^{254.4}$	2^8	2^{40}

- ▶ Known data: chosen pairs of (plaintext, ciphertext)
- ▶ MITM: Meet-in-the-middle
- ▶ Lucks: S. Lucks, Attacking Triple Encryption, in *Fast Software Encryption*, Springer, 1998
- ▶ Biclique: Bogdanov, Khovratovich and Rechberger, Biclique Cryptanalysis of the Full AES, in *ASIACRYPT2011*, Springer, 2011

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