

# Random Number Generators

## Examples

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### 1 Linear Congruential Generator

$$X_{n+1} = (aX_n + c) \bmod m$$

#### 1.1 Example 1

$$a = c = 1; m = 100$$

$$X_0 = 23$$

$$\begin{aligned} X_1 &= (23 + 1) \bmod 100 \\ &= 24 \end{aligned}$$

$$\begin{aligned} X_2 &= (24 + 1) \bmod 100 \\ &= 25 \end{aligned}$$

Sequence will be: { 24, 25, 26, 27, ... 99, 0, 1, 2 }

#### 1.2 Example 2

$$a = 7, c = 0, m = 32$$

$$X_0 = 1$$

$$\begin{aligned} X_1 &= (7 + 0) \bmod 32 \\ &= 7 \end{aligned}$$

$$\begin{aligned} X_2 &= (7 \times 7 + 0) \bmod 32 \\ &= 17 \end{aligned}$$

$$\begin{aligned} X_3 &= (7 \times 17 + 0) \bmod 32 \\ &= 23 \end{aligned}$$

$$\begin{aligned} X_4 &= (23 \times 7 + 0) \bmod 32 \\ &= 1 \end{aligned}$$

$$X_5 = 7$$

Sequence will be: { 7, 17, 23, 1, 7, 17, 23, 1, ... } only uses 4 out of 32 values

#### 1.3 Example 3

$$A = 5, c = 0, m = 32$$

$$X_0 = 1$$

$$X_1 = 5$$

$$X_2 = 5 \times 5 \pmod{32} \\ = 25$$

$$X_3 = 25 \times 5 \pmod{32} \\ = 29$$

$$X_4 = 29 \times 5 \pmod{32} \\ = 17$$

Sequence will be: {5, 25, 29, 17, 21, 9, 13, 1, 5, ... }